Insulin Administration for People with Type 1 diabetes

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Abstract
In this paper, we apply model predictive control (MPC) for control of blood glucose in people with type 1 diabetes. The two first control strategies are based on nonlinear model predictive control (NMPC). The first control strategy is based on meal announcement in advance, while the second one considers meal announcement at mealtimes only. They give a quantitative upper bound on the achievable control performance. The third control strategy is a feedforward-feedback control strategy. This strategy uses a time-varying setpoint to reduce the risk of hypoglycemia. The feedback controller computes the optimal basal insulin infusion rate. The feedforward controller consists of a bolus calculator. It computes the optimal bolus, along with the time-varying glucose setpoint. We test these three strategies on a virtual patient with type 1 diabetes. The numerical results demonstrate the robustness of the last control strategy with respect to changes in the model parameters and incorrect meal announcement.

Keywords: Type 1 diabetes, Nonlinear model predictive control, feedforward-feedback control

1. Introduction
The World Health Organization (WHO) estimates that more than 220 million people worldwide have diabetes. This number is likely to double by 2030. In the USA, the budget for diabetes represents 10% of the health care budget, i.e. more than 130 billion dollars (132 billion dollars in 2002).
In people without diabetes, the blood glucose is controlled tightly around 90 mg/dL (5 mmol/L). Type 1 diabetes is a chronic disease characterized by an insufficient (effectively nonexistent) endogenous production of insulin, which leads to poor regulation of glucose concentrations in the blood. In particular, the deficiency of insulin causes sustained high glucose levels (hyperglycemia) that result in serious long-term health problems like eye, nerve, and kidney disease. On the other hand, too much insulin can result in very low glucose levels (hypoglycemia) which can pose immediate health risks. Consequently, exogenous insulin must be injected to regulate the blood glucose concentration as tightly as possible.
Usually, insulin treatment consists of the administration of rapid acting insulin through boluses (i.e., discrete insulin administration) at the time of meals. The size of the bolus is based on a measurement of the current blood glucose at mealtime and the (estimated) size of the meal. However, having measurements only at mealtime does not provide enough information about blood glucose. Consequently, people with diabetes often tolerate hyperglycemia in order to avoid hypoglycemia and its immediate effects.
Continuous glucose monitors (CGM) can help to provide a better control of blood glucose. They measure the glucose concentration in the subcutaneous depot. Insulin pumps that continuously inject fast acting insulin have also been developed. Combining a CGM with an insulin pump can enable automatic insulin administration for people with type 1 diabetes. Such a medical device is called an artificial pancreas, and its principle is illustrated in Fig. 1. Several research groups work on aspects of control algorithms integrating the CGM and the insulin pump to automatically adjust insulin administration for people with type 1 diabetes, such as Cobelli et al. (2009) and Klonoff et al. (2009).

In this paper we use the model developed by Hovorka et al. (2004) and described in Boiroux et al. (2010b) to simulate a patient with type 1 diabetes. In the Hovorka model, the quality of the glucose control is limited by the time lag associated with subcutaneous-to-intravenous insulin absorption. This system property fundamentally limits the control quality that can be achieved in closed-loop insulin administration, as demonstrated in Boiroux et al. (2010a).

2. Nonlinear Model Predictive Control

In this section, we state the continuous-time optimal control problem and apply it to the computation of the optimal insulin profiles for people with type 1 diabetes. The optimal insulin administration is formulated as a bound constrained continuous-time Bolza problem

\[
\min_{[x(t),u(t)]_{t_0}^{t_f}} \phi = \int_{t_0}^{t_f} g(x(t),u(t))dt + h(x(t_f))
\]

subject to

\[
x(t_0) = x_0 \\
\dot{x}(t) = f(x(t),u(t),d(t)) \\
u_{\min} \leq u(t) \leq u_{\max}
\]

in which \(x(t) \in \mathbb{R}^n\) is the state vector, \(u(t) \in \mathbb{R}^m\) is the vector of manipulated inputs (insulin injection), and \(d(t) \in \mathbb{R}^p\) is the vector of known disturbances (meals). We assume the state vector \(x(t)\) and the input vector \(u(t)\) to be constant between the sampling times and a constant sampling time \(T_s = 5\) min. Thus, we can use the multiple-
In this section we describe an offset-free feedforward-feedback controller to compute optimal insulin profiles. Garcia-Gabin et al (2008) and Marchetti et al. (2008) established that a time-varying glucose setpoint can reduce the risk of hypoglycemia. The feedforward controller consists of a bolus calculator. It computes the optimal bolus size and the glucose setpoint, based on the meal size announced by the patient. The feedback controller adjusts the basal insulin infusion rate to compensate for mismatches in meal announcement and variations in the physiological parameters of the patient. The calculation of the basal insulin is based on a linear MPC algorithm.

We use the Hovorka model and the offset-free linear MPC algorithm developed in Boiroux et al. (2011) to compute the optimal insulin administration profiles for people with type 1 diabetes. In the scenario considered, the glucose sensor provides a signal perturbed by a normally distributed white noise. We consider two cases. In the first case, we decrease the insulin sensitivity by 50% under fasting conditions. In the second
In this paper we applied nonlinear model predictive control to compute the optimal insulin profiles for people with type 1 diabetes. These profiles give an upper-bound on the maximal achievable performance in the cases where the meals are announced beforehand, and in the case where meals are announced at mealtimes only. We utilized the bolus-like nature of the optimal insulin profile to design an offset-free feedforward-feedback controller. The feedforward part is a model-based bolus calculator, while the
feedback part adjusts the basal insulin infusion rate. The numerical results demonstrate that a rather good control of blood glucose can be obtained, assuming that a fairly good physiological model of the patient can be identified.

References


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